



Wavelet Analysis for Processing of Earthquake Records

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ABSTRACT

Nonlinearities are often encountered in the analysis and processing of real-world signals. Most existing approaches to nonlinear signal processing characterize the nonlinearity in the time domain or frequency domain. In fact, there are good reasons for characterizing nonlinearity using more general signal representations like the wavelet expansion. Wavelet expansions often provide very concise signal representation and thereby can simplify subsequent nonlinear analysis and processing. Wavelets also enable local nonlinear analysis and processing in both time and frequency, which can be advantageous in non-stationary signals. The Wavelet Transform technique is particularly suitable for non-stationary signals like Earth Quake. In contrast to the Fourier Transform, the wavelet transform allows exceptional localization, both in the time domain via translation t of the wavelet, and in the frequency domain via dilations scales b , which can be changed from minimum to maximum, chosen by the user. The Wavelet Transform technique is able to detect the complex variability of Earth Quake signals in time–frequency space.

Keywords: *Nonlinearity, Non-stationary Signals, Wavelet Transform, Earth Quake, Fourier Transform*

I. INTRODUCTION

The earthquake records are the time-domain signals. However, in many cases the most distinguished information is hidden in the frequency spectrum, which provides the energy, associated with a given frequency. The frequency spectrum of the signal can be obtained by the Fourier Transform (FT). The FT yields information on how much but not when (in time) the particular frequency components exist. Such information is sufficient in a case of the stationary signals as the frequency content of such signals does not change in time and all frequency components exist all the time. However, in all cases the earthquake waves change in a relatively short period of time [1].

When waves start to break, the frequency content of signal changes rapidly in time due to nonlinear interaction between elementary wave components and resulting energy transfer, and energy dissipation. In such cases, the FT provides information on the frequency content; however, the information on the frequency localization in time is essentially lost in the process. When the time localization of the spectral components is required, the transform of time series, which provides the time–frequency representation of the signal, should be developed. Transform of such type is the wavelet transform, which gives full time–frequency representation of the time series. In contrast to the FT, the wavelet transform allows exceptional localization in the time domain via translations of the so called mother wavelet, and in the scale (frequency) domain via dilations [2-3].

Wavelet transform is a relatively modern technique and in recent years enormous interest in the application of wavelets has been observed. On the other hand, the application of the wavelet transform to earthquake engineering is not frequent. Discrete and fast wavelet transforms are used for dynamic analysis of structures induced earthquake load. Then the discrete and fast wavelet transform are used for optimization of structures with earthquake loading [4-5].

In this paper the application of wavelet transform for the processing of earthquake record is discussed and an attempt to produce some useful quantitative results is made. The fundamentals of the WT are given and the difference between FT and WT is demonstrated and the application of the WT for processing of earthquake record is shown.

The paper is organized as follows. Section II gives the brief introduction of earth quake signals. Section III present the over view of Fourier Transform. Section IV gives information about Wavelet Transform. Section V describes the proposed Wavelet Transform system. Finally some conclusions are reported in Section VI.

II. EARTH QUAKE

The structure of Earth's deep interior cannot be studied directly. But geologists use seismic (earthquake) waves to determine the depths of layers of the molten and semi-molten material within Earth. Because different types of earthquake waves behave differently when they encounter material in different states (for example, molten, semi-molten, solid), seismic stations established

around Earth. detect and record the strengths of the different types of waves and the directions from which they came. Geologists use these records to establish the structure of Earth's interior.

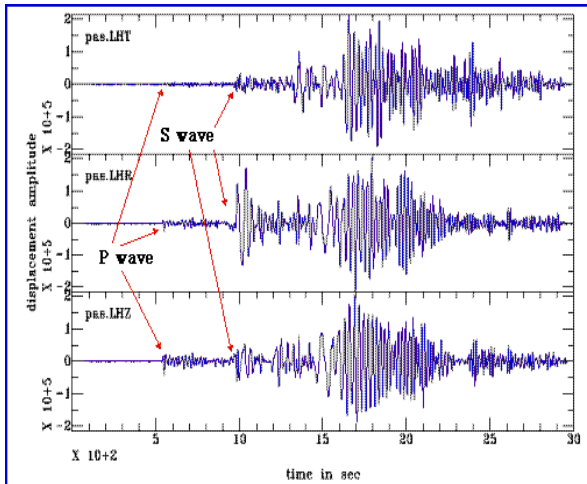


Fig.1: Earth Quake Signals

The two principal types of seismic waves are P-waves (pressure; goes through liquid and solid) and S-waves (shear or secondary; goes only through solid - not through liquid). The travel velocity of these two wave types is not the same (P-waves are faster than S-waves).

Thus, if there is an earthquake somewhere, the first waves that arrive are P-waves. In essence, the gap in P-wave and S-wave arrival gives a first estimate of the distance to the earthquake. Fig. 1 shows some typical seismograms with arrival of P- and S-waves marked [7].

III. FOURIER TRANSFORM

Transform of a signal is just another form of representing the signal. Transform does not change the information content present. Mathematical transform are applied to signal to obtain further information which is not present in raw signal. The FT is probably the most popular transform being used, but for better understanding the difference between the WT and the FT, a short overview of the FT is provided. In the FT there is no resolution problem in the frequency domain, as we know exactly what frequencies exist. This perfect frequency resolution in the FT is due to the fact that the window used in this transformation, lasts all the time, from minus infinity to plus infinity. Similarly, there is no time resolution problem in the time domain, since we know the value of the signal at every instant of time. In contrary, we can say that both time resolution in the FT and the frequency resolution in the time domain are zero, since we have no information about them [1].

IV. WAVELET TRANSFORM

The WT is similar to the FT as it breaks a signal down into its constituents. Whereas the FT breaks the signal into a series of sine waves of different frequencies, the WT breaks the signal into its wavelets, which are scaled and shifted versions of the so called mother wavelet. The WT allows exceptional localization both in the time domain via translations of the wavelet, and in the frequency (scale) domain via dilations. The wavelets are complex or real functions concentrated in time and frequency and having the same shape. In the WT, the signal is multiplied with the wavelet, and the transform is separately computed for different segments of the time domain signal [1].

For a better understanding of the wavelet transform nature, the relation between the wavelet transform and the more common Fourier transform is the basic one for the interpretation of the results of processing of the signals by the wavelet technique. This relation is not straightforward for arbitrary wavelet. However, in the case of the Morlet wavelet used in this paper, the relationship between WT and FT can be found in a simpler way, mainly due to the periodic character of the Morlet's wavelet [6].

V. PROPOSED WAVELET TRANSFORM SYSTEM

Wavelets are now days very popular in predicting and analyzing the non-linearity in the Natural process, which needs to be modeled. As the popularity of MATLAB is also growing, the wavelet toolbox will allow us to efficiently analyze the unknown waveform and to predict the future occurrences also. It is aimed at improving the older techniques and to get a more reliable pattern matching. In this system we are taking input data from sensors. Our aim is to find out distance of earth quake centre to the earth quake station and analyze the different frequency components in signal. Fig. 2 shows the block diagram of proposed wavelet transform system.

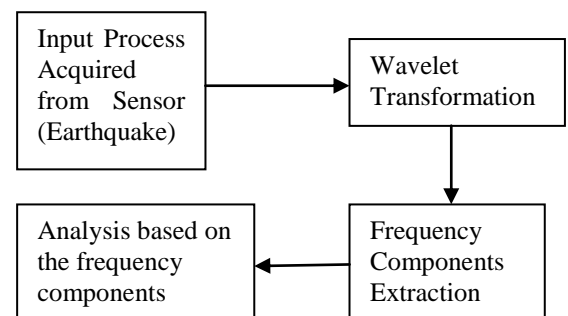


Fig.2. Block Diagram of the Proposed Wavelet Transform System

A. Processed Data of Earth Quake

In this section, FT and WT of the Taft earthquake will be computed. The earthquake record and FT of the Taft are shown in Fig. 3 and 4, respectively. WT of the earthquake record in two dimensions is shown in Fig. 5. By comparing Figures 4 and 5, it is observed that the highest frequency of the earthquake record is 1.5 (Hz), which is corresponding to scale 0.68. Besides, the frequency range of 1.25-1.8 (Hz) has the most important of FT, is the same as the highest frequency range. On the other hand, we can say that the frequency range of 1.25-1.8 can be the same as the scale range of 0.55- 0.8. Referring to Figures 5, the output programming for this purpose, we can distinguish the time of each frequency. For example, the time of the frequency 1.5 which is as correspond to scale 0.68, is 1.348 seconds. The time of the frequency range 1.25-1.8, is 13.2-14.1 seconds. In other words, this range of time is the most dangerous range for all constructions which have the same frequency as the dominant frequency of earthquake. The important frequency of the Taft earthquake is 1.5 Hertz. This frequency equals to frequency of steel frame with the heights of 17m. For this particular construction, the resonance takes place due to the closeness of the frequency of the construction with the frequency of the earthquake at 13.48 seconds after the beginning of the earthquake and in theoretically the construction is destroyed. In the same way, we can compute the time of other frequencies of the earthquake record.

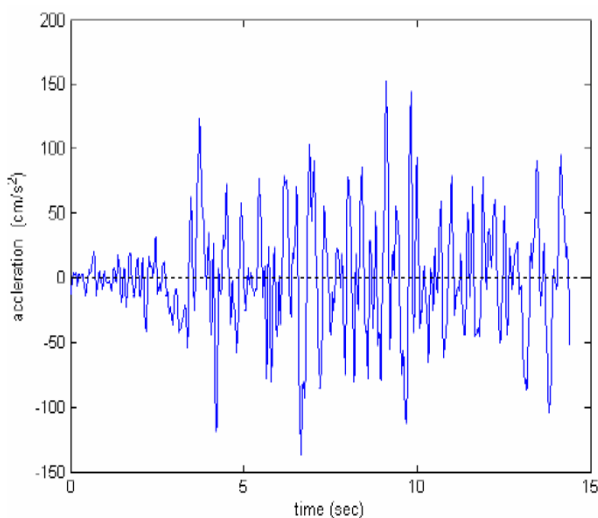


Fig.3: Taft Earth Quake Records

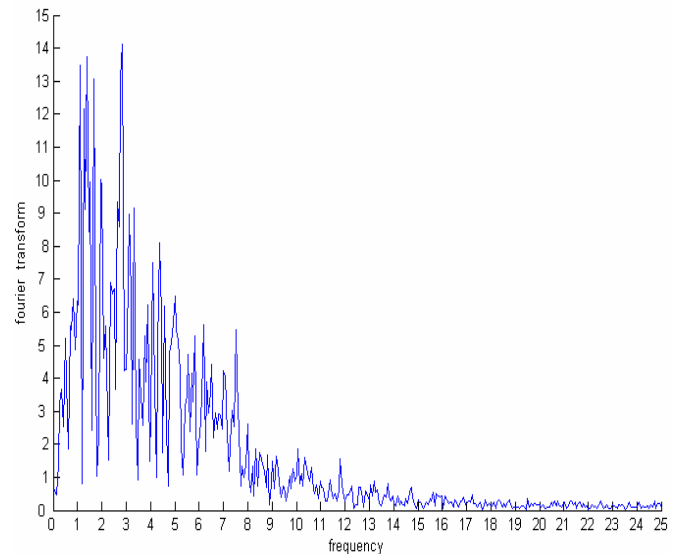


Fig.4: FT of Taft Earth Quake Records

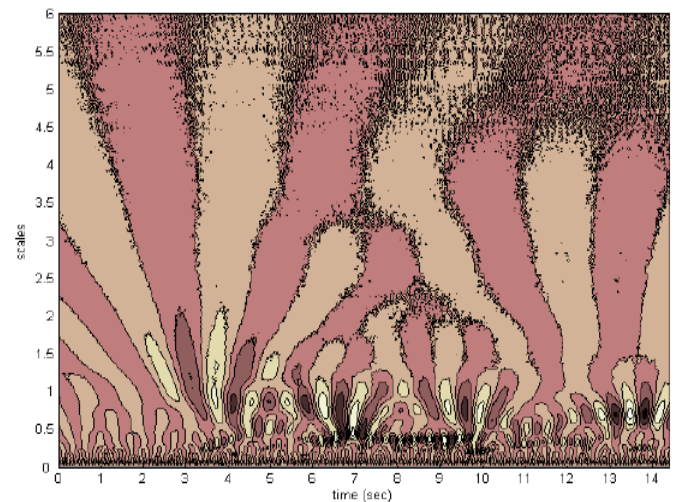


Fig.5: Two dimensional WT of Taft Earth Quake Records

VI. CONCLUSION

The wavelet transform technique is particularly suitable for non-stationary signals. In contrast to the Fourier transform, the wavelet transform allows exceptional localization, both in the time domain via translation t of the wavelet, and in the frequency domain via dilations scales b , which can be changed from minimum to maximum, chosen by the user. The variations of the frequencies corresponding to the maximum of the wavelet transform at particular time are very similar to the recorded frequencies. It is interesting to note that wavelet transform shows the influence of the some low frequency components which are not clearly seen in the classical energy spectrum.



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